DGR: Differentiable Global Router

Abstract

Modern VLSI design flows necessitate fast and high-quality global routers. In this paper, we introduce DGR, a GPU-accelerated, differentiable global router capable of concurrent optimization for millions of nets, which we aim to open-source. Our innovation lies in the development of a routing Directed Acyclic Graph (DAG) forest to represent the 2D pattern routing space for all nets, enabling coordinated selection of Steiner trees and 2-pin routing paths from a global perspective. For efficient search within the DAG forest, we relax the discrete search space to be continuous and develop a differentiable solver accelerated by deep learning toolkits on GPUs. Experimental results demonstrate that DGR substantially mitigates routing overflow while concurrently reducing total wirelengths from 0.95% to 4.08% in congested testcases compared to state-of-the-art academic global routers. Additionally, DGR exhibits favorable scalability in both runtime and memory with respect to the number of nets.

1 Introduction

The continuously shrinking technology node has led to a notable increase in the density and scale of VLSI circuits, posing substantial challenges for routing algorithms. To manage this complexity, VLSI routing has been divided into two sub-problems: global routing, which focuses on generating coarse-grain routing guides, and detailed routing, where routing tracks are assigned for all connections guided by these routing guides while ensuring compliance with design rule constraints. The outcome of global routing plays a pivotal role in shaping the efficiency of detailed routing and the overall quality of post-route circuits. Additionally, the efficiency of global routing is crucial, as it contributes to streamlining timingand congestion-driven floor-planing and placement by providing accurate interconnect information [1]. Thus, modern VLSI design workflows require fast and high-quality global routing algorithms.

A Directed Acyclic Graph (DAG)-based global router called CUGR2 is proposed in [2] and achieves state-of-the-art results in the academic community. Figure 1 depicts the construction of a routing DAG, which serves as the data structure for representing available pattern routing paths for a net. Initially, a rectilinear Steiner minimum tree (RSMT) [3] connects all pins, breaking the multi-pin net into 2-pin sub-nets (Figure 1b). Subsequently, routing paths conforming to available patterns are established for each 2-pin sub-net. The final routing DAG (depicted in Figure 1c) comprises vertices representing pins, Steiner points, or turning points, and edges representing interconnect wire segments within routing paths. CUGR2 optimizes one net at a time, employing a dynamic programmingbased algorithm to determine the best pattern routing paths and layer assignments. However, CUGR2 does not guarantee optimal solution among all nets because of its sequential heuristic. Moreover, its sequential heuristic falls short in addressing routing congestion from a global perspective, possibly leading to unnecessary iterations of rip-up and reroutes. Combinatorial optimization-based techniques [4, 5] could help concurrent optimize multiple nets. But they are often too slow for modern VLSI circuits.

In this work, we propose a novel <u>Differentiable Global Router</u>, named **DGR**, to enable concurrent optimization of millions of nets. It involves the creation of a **routing DAG forest** (depicted in Figure 2 (a)) to concisely represent the 2D pattern routing space for all



Figure 1: An example from a multi-pin net (a) to routing DAGs (c or d). (b) is the rectilinear Steiner minimum tree (RSMT) by FLUTE. Edges in a CUGR2 DAG represent interconnect wire segments, whereas edges in a DGR DAG symbolize potential 2D routing paths for 2-pin sub-nets.



Figure 2: Differentiable search in a DAG forest. (a) Optimal selection of routing tree topologies and 2-pin routing paths are initially unknown. (b) Continuous relaxation of the search space by placing a probability on each routing tree topology candidate and each 2-pin path candidate. (c) Optimization of the probabilities in a differentiable manner. (d) Inducing the final routing trees from the optimized probabilities.

nets. It is an abstraction, adaption and extension of the DAG concept in [2]. Here, a single net may be associated with multiple routing DAGs, with each DAG signifying a distinct routing tree topology candidate for that net. Within each routing DAG, individual edges symbolize potential 2D routing path candidates for 2-pin sub-nets. With a DAG forest, the 2D global routing problem is formulated as selecting a routing DAG for each net, followed by choosing one 2-pin path for each 2-pin sub-net within the DAG, such that the total wire length, via count and overflow are minimized. To enable scalable and effective search within the DAG forest, we relax the discrete search space to be continuous and develop an end-to-end differentiable solver (as shown in Figure 2) accelerated by deep learning toolkits on GPUs. Additionally, we introduce a Gumbel-Softmax technique with temperature annealing and top-p selection to bridge the gap between the continuous search space and discrete routing solutions. We summarize our contributions as follows:

- We propose a GPU-accelerated differentiable global routing framework, named DGR, designed for concurrent optimization for millions of nets. To our best knowledge, it is the first GPU-accelerated concurrent global router.
- We propose establishing a routing DAG forest to represent the search space encompassing routing tree topologies and 2-pin routing paths for all nets in a given layout. This facilitates the coordinated selection of Steiner trees and routing paths for all nets from a global perspective.
- We propose a differentiable algorithm for scalable and efficient search within the DAG forest. Gumbel-Softmax technique with temperature annealing and top-p selection are introduced to further enhance the solution quality.
- Experimental results demonstrate DGR can be easily scaled to solve a million-level benchmark, and outperforms the state-of-the-art academic global routers.

2 Prior Works

Global routing approaches can be categorized into two major groups: concurrent [5-7] and sequential [8? -12], based on whether they handle one or multiple nets simultaneously. Sequential methods often utilize a "rip-up and reroute" framework [1]. They commence with an initial routing solution and then iteratively improve it, addressing one net at a time. In each iteration, a net that traverses a congested area is removed (rip-up) and subsequently rerouted to bypass the congested regions. The sequencing of net routing plays a vital role in determining the ultimate routing quality. And sequential approaches can stagnate on local minima due to their refinement heuristics. On the other hand, concurrent approaches try to handle multiple nets simultaneously. They are generally based on combinatorial optimization techniques, such as multicommodity flow [4] and integer linear programming [5-7]. While concurrent techniques have demonstrated their ability to yield superior routing outcomes, particularly in challenging routing scenarios, they often exhibit noticeably slower computational speeds in contrast to sequential methodologies. Recently, GPU-accelerated global routing [10-12] has garnered considerable attention, achieving approximately a tenfold increase in speed while maintaining routing quality. However, the majority of these approaches rely on "parallelizing" traditional sequential algorithms in GPUs. While these methods significantly enhance runtime, the quality of the routing result is still limited by the traditional sequential-based algorithms. Our work falls within the realm of concurrent approaches, yet it not only tries to deliver superior performance but also good scalability comparable to sequential methods by effectively harnessing the massive parallelism offered by GPUs in a distinct novel way.

Another categorization of global routing is based on the dimensionality of routing: 2D [5–8] and 3D [2, 9–12]. In 2D global routing, routing is confined to the horizontal and vertical directions, necessitating a subsequent assignment of routing layers for each wire. Conversely, 3D global routing spans all three spatial dimensions, determining wire layers within the routing process. In theory, 3D routing offers the potential for superior solutions by enabling more efficient utilization of 3D routing resources. However, in practice, 2D approaches often achieve comparable quality results with significantly shorter runtime. Thus, our work adopts the 2D approach.

3 Formulation of Pattern Routing Based on DAG Forests

3.1 Routing DAG Forest

A routing DAG forest is a mathematical structure to systematically describe the 2D pattern routing space for all the nets. A single net may be associated with multiple routing DAGs, with each DAG signifying a distinct routing topology for that net. In each routing DAG, vertices denote pins and Steiner points, and edges represent potential 2D routing paths for two-pin sub-nets within the specified routing topology. These paths can take various forms, including L-/Z-/C-shape pattern routing, monotonic routing, or even maze routing. The realization of a 2D pattern routing solution entails the selection of a routing DAG for each net, followed by finding one routing path for each 2-pin sub-net within the DAG, as shown in Figure 2 (d). In contrast to CUGR2 [2], which addresses one net at a time and focuses on a single Steiner tree topology in each instance, our routing DAG forest allows multiple DAGs for each net and facilitates the coordination of DAG and DAG edge selection across all nets in a global view.

The construction of the DAG forest has a direct impact on the runtime and quality of DGR outcome. Section 4.2 will illustrate how we construct the DAG forest in this work. As a future direction, we plan to explore the adaptive expansion of the forest by introducing new DAGs and DAG edges for nets in congested areas when necessary.

3.2 Formulation of Pattern Routing

This work focuses on 2D pattern routing. The dynamic programmingbased layer assignment and maze routing-based refinement presented in [2] are applied to our pattern routing outcome to generate the final 3D routing solution. Given a routing DAG forest constructed by techniques in Section 4.2, the objective of 2D routing is to select the best routing DAGs (routing trees) and DAG edges (2-pin paths) for all the nets such that the total wire length, number of vias, and routing overflow are minimized. Before delving into the problem formulation, we need to define some terminology:

Let N be the set of input nets. the first task is to construct a routing DAG forest $\mathcal{F} = \{\mathcal{T}, \mathcal{S}, \mathcal{P}\}\)$, where \mathcal{T} is the routing tree candidate pool, \mathcal{S} is the set of 2-pin sub-nets in all routing trees, and \mathcal{P} represents 2-pin path candidate pool. Let $i \in \mathcal{P}$ be a specific 2-pin path candidate, then $subnet(i) \in \mathcal{S}$ denotes the corresponding 2-pin sub-net of i, $tree(i) \in \mathcal{T}$ denotes the corresponding routing tree of i, and $x_i \in \{0, 1\}$ is the binary indicator about whether i is selected, i.e., $x_i = 1$ if and only if i is selected after global routing. Let $j \in \mathcal{T}$ be a specific routing tree candidate, then $net(j) \in \mathcal{N}$ denotes the corresponding net of j, and $y_j \in \{0, 1\}$ is the binary indicator about whether j is selected, i.e., $y_j = 1$ if and only if j is selected after global routing.

Let \mathcal{E} be the set of all g-cell edges, and $e \in \mathcal{E}$ be a specific g-cell edge. The capacity of *e*, denoted as cap_e , can be formulated as:

$$cap_e = track_e - \beta_v pin_density_v - local_net_e$$
 (1)

Where:

- track_e is the the number of available tracks in e.
- pin_density_v is the number of pins in the g-cell v which is connected to e in the g-cell graph.
- β_v is a weight from CUGR2, based on the minimal edge length and defined in the LEF file and physical length of edges connecting v.

 local_net_v denotes the number of local nets at v, i.e., nets only occupying v.

In the capacity formula, the second part $(\beta_v pin_density_v)$ and the third part $(local_net_e)$ are used to estimate the influence of pin connections and local nets, which are essential for final detailed routing quality.

The demand of e, d_e , is given by:

$$d_e = \sum_{i \in \mathcal{P}_e} y_{tree(i)} x_i + \beta_v \left(\sum_{k \in \mathcal{P}_v} y_{tree(k)} x_k \right)$$
(2)

Where:

- \mathcal{P}_e is the set of 2-pin path candidates passing through e.
- \mathcal{P}_v is the set of 2-pin path candidates with a turning point at v.
- *β_v* is a weight following the same definition as above.

The demand calculation comprises two parts: the first part models the influence of the wires that go through the edge, and the second part represents the influence of vias.

Given the above definitions, the DAG forest-based 2D pattern routing problem can be mathematically formulated as follows:

$$\min_{i \in \mathcal{P}, j \in \mathcal{T}} a_1 \times \mathsf{WL_cost} + a_2 \times \mathsf{via_cost} \\ + a_3 \times \mathsf{overflow_cost}$$

(3)

s.t.
$$WL_{cost} = \sum_{i \in \mathcal{P}} y_{tree(i)} x_i WL_i$$
, (4)

$$via_cost = \sqrt{L} \sum_{i \in \mathcal{P}} y_{tree(i)} x_i TP_i,$$
(5)

$$overflow_cost = \sum_{e \in \mathcal{E}} f(cap_e - d_e), \tag{6}$$

$$\sum_{subnet(i)=s} x_i = 1, \forall s \in \mathcal{S},$$
(7)

$$\sum_{j:net(j)=n} y_j = 1, \forall n \in \mathcal{N},$$
(8)

where a_1, a_2 and a_3 are the weights for wire length cost, via cost, and overflow cost, respectively. WL_i is the wire length of the 2-pin path candidate *i*, and TP_i is the number of turning points of *i*. *L* is the number of routable layers. f(*) represents some non-linear function to be applied to the resource (capacity - demand) of g-cell edges, e.g., the ReLU function used in [13] and logistic function used in [2, 9]. Equation (7) ensures the selection of a single path for each 2-pin sub-net. Similarly, Equation (8) guarantees the selection of a single routing tree for each net.

4 Differentiable Global Router

4.1 DGR Workflow

i:

Figure 3 depicts the DGR workflow. Initially, we construct a DAG forest, encompassing routing tree candidates and 2-pin path candidates for each 2-pin sub-net within the trees. Every candidate is associated with a "selection" probability and the expctation of the costs defined in Equation (3) to Equation (6) are derived based on these probabilities. Subsequently, the selection probabilities are updated through back-propagation of the costs. This iterative process continues until the iteration limit is reached. The 2D pattern routing solution is then obtained by selecting routing tree and 2-pin path candidates according to the optimized probabilities. This solution further undergoes dynamic programming-based layer assignment



Figure 3: The workflow of DGR.

and maze routing-based refinement, as detailed in [2], to ultimately generate the final 3D global routing solution.

4.2 Routing DAG Forest Construction

The routing DAG forest comprises routing tree candidates for each net, with each of these tree candidates spawning a collection of 2-pin path candidates. An example of the constructed DAG forest is provided in Figure 4. Initially, multiple routing tree candidates are formulated for each net using FLUTE and its fine-tuned version by CUGR2, which moves Steiner points based on congestion. It's worth noting that this is not restricted to just these two techniques; alternative routing tree generation algorithms, such as SALT [14] and TreeNet [15], can seamlessly integrate their resulting trees as additional candidates. Subsequently, every routing tree is used to segment the multi-pin net into 2-pin segments based on its tree topology. Then, all L-shape pattern paths are enumerated for each 2pin sub-net and incorporated into the pool as 2-pin path candidates. In the final step, each candidate will be associated with a probability, which is initialized randomly.

4.3 Continuous Relaxation and Cost Calculation

We relax the categorical choice of candidates (x_i, y_j) to selection probabilities. Formally, we define $p_i \in [0, 1]$ as the probability of selecting 2-pin path candidate *i*, and $q_j \in [0, 1]$ as the probability of selecting the routing tree topology candidate *j*. Then, the expectation of the costs in Section 3.2 can be calculated as:

$$overflow_cost = \sum_{e \in \mathcal{E}} f(cap_e - d_e)$$
(9)

i.e.,
$$d_e = \sum_{i \in \mathcal{P}_e} q_{tree(i)} p_i + \beta_v (\sum_{k \in \mathcal{P}_v} q_{tree(k)} p_k)$$
(10)

wirelength_cost =
$$\sum_{i \in \mathcal{P}} q_{tree(i)} p_i WL_i$$
(11)

$$via_cost = \sqrt{L} \sum_{i \in \mathcal{P}} q_{tree(i)} p_i \mathsf{TP}_i$$
(12)

The total cost is a weighted sum of overflow cost, wirelength cost, and via cost. In our experiments, we adopt the metric weights from the ICCAD'19 contest: $cost = 500 \times overflow_cost + 4 \times via_cost + 0.5 \times wirelength_cost$. Figure 4 illustrates the workflow to compute the cost.



Figure 4: Workflow for cost calculation. Segments of the via cost flow (in red) and wirelength cost flow (in purple), are omitted for simplicity.

4.4 Differentiable Optimization

We cannot, unfortunately, directly optimize the costs defined in Equation (9) to Equation (12) with respect to the probabilities due to the following constraints:

$$\sum_{\substack{subnet(i)=s\\net(j)=n}} p_i = 1, \forall s \in \mathcal{S}; \forall p_i \in [0, 1]$$

To transform the constrained optimization problem into an unconstrained one, we introduce an auxiliary layer to map unconstrained trainable variables ($w = \{w_i \in \mathbb{R}\}$) to probabilities, as depicted in Figure 4. A softmax layer seems to be an intuitive fit:

$$p_i = \frac{\exp(w_i)}{\sum_{k:tree(k)=tree(i)} \exp(w_k)}$$
$$q_j = \frac{\exp(w_j)}{\sum_{k:net(k)=net(j)} \exp(w_k)}$$

However, softmax deterministically samples a probability distribution. This deterministic nature can inadvertently lead to local optima, especially when the probabilities have a bad initialization. To circumvent this, we employ the gumbel_softmax function [16]:

$$p_i = \frac{\exp\left((w_i + g_i)/t\right)}{\sum_{k:tree(k)=tree(i)} \exp\left((w_k + g_k)/t\right)}$$
$$q_j = \frac{\exp\left((w_j + g_j)/t\right)}{\sum_{k:net(k)=net(j)} \exp\left((w_k + g_k)/t\right)}$$

This function, a stochastic variant of softmax, introduces Gumbel noise (g_i) , i.e., the sample from the Gumbel distribution, to the logits prior to applying the softmax operation. Furthermore, to ensure that the final sampling of the routing tree candidate is discrete, we progressively reduce the temperature (t) of the gumbel_softmax throughout the iterations, called temperature annealing. It ensures

that the final probabilities associated with routing tree candidates closely approximate either 0 or 1.

We have implemented our differentiable solver within the DGR framework using the deep learning toolkit *PyTorch*, as visualized in Figure 3. Leveraging *PyTorch*, we benefit from its robust and efficient support for matrix operations, automatic gradient derivation, and optimization. This toolkit seamlessly integrates GPU acceleration, further enhancing computational efficiency and enabling rapid experimentation in our research efforts.

4.5 Deriving Discrete Selection

When the maximum iteration count is reached, a 2D routing solution is derived by selecting candidates based on their associated probabilities.

Among the routing tree candidates, the one with the highest probability is selected. This probability tends to approach 1 as a result of our temperature annealing technique.

For 2-pin path candidates, we employ top-p sampling [17]. Initially, candidates are ranked by their probabilities. Subsequently, top candidates are selected until their cumulative probability surpasses a predefined threshold.

4.6 Post-Processing

Our 2D pattern routing solution will undergo dynamic programmingbased layer assignment introduced in [2] to yield preliminary 3D routing results. Subsequently, maze routing is applied to nets in congested areas to further minimize overflow. The final output is a comprehensive guide for detailed routing.

5 Experiments

We implement DGR using PyTorch. Experiments are conducted on a 64-bit Linux workstation with Intel Xeon Silver 2.20 GHz CPUs and 256 GB memory. One NVIDIA GeForce RTX 2080Ti graphics card is used. We use the benchmarks from ICCAD'18 and Table 1: Comparison with ILP on synthetic data. DGR best/worst is the best/worst result among five runs with different random seeds, respectively. DGR* is the best result after the hyper-parameter search, i.e., additional 100 runs that randomly sample learning rate from 10^{-4} to 1 and temperature scaling factor in [0.8,0.85,0.9,0.95].

Synthetic data parameters					Runtime (s)		Overflow				
	Grid Graph	cape	Net #	box size	ILP	DGR	ILP	DGR*	DGR best	DGR worst	
	20×20	1	20	4	0.08	5.09	30	30	30	30	
	50×50	1	50	10	36.12	5.16	173	173	173	173	
	50×50	1	100	10	102.46	4.95	1028	1028	1028	1028	
	50×50	2	100	10	38.79	4.89	0	0	0	0	
	50×50	1	1000	10	4621.12	5.59	35445	35445	35445	35445	
	50×50	10	1000	10	2493.21	78.85	7407	7407	7407	7407	
	50×50	10	10000	10	N/A	81.24	N/A	364536	364536	364621	
	100×100	2	1000	20	5763.16	5.83	48846	48846	48849	48891	
	100×100	2	10000	20	N/A	75.90	N/A	785664	785664	785678	
	1000×1000	1	100000	200	N/A	924.23	N/A	80237614	80238208	80249124	
				Ratio	>118.28	1.00	1.00	1.00	$>1 - 10^{-6}$	>1 - 10 ⁻⁵	

ILP is implemented via CVXPY [21]. The green indicates that the result is as optimal as ILP method. N/A means ILP is running out of the time (> 8 hours).

ICCAD'19 contests [18]. The activation function f is sigmoid by default. We use Adam to optimize the weights w, with the initial learning rate 0.3. w is initialized randomly, and the random seed is fixed if not mentioned. The iteration number is 1000, and the initial temperature is 1. For every 100 iterations, we scale down the temperature by a factor of 0.9.

5.1 Comparison with ILP: Proof of Concept

To understand the gap between the differentiable-based method and the optimal solution, we first compare DGR with Integer Linear Programming (ILP) based method. Since the benchmarks in ICCAD'19 are too large to be completed timely for ILP, synthetic data is employed for this experiment. Specifically, three G-cells are arbitrarily selected within a box for each net, designating them as pins. Both ILP and DGR are tasked with selecting the L-shaped path candidate for every 2-pin pair to minimize overflow. The overflow is calculated using ReLU, i.e., overflow = $\sum_{e \in \mathcal{E}} \text{ReLU}(d_e - cap_e)$, given that ILP does not support alternative non-linear functions. DGR directly picks the path with the largest probability. The results are shown in Table 1. Remarkably, when equipped with the appropriate hyper-parameter (DGR*), DGR mirrors ILP's result quality. Even in the absence of hyper-parameter optimization, the overflow disparity between ILP and the least favorable DGR seed remains below 10^{-5} .

5.2 Comparison with Leading Global Routers

We compare the global routing results of DGR with those of CUGR2 on the most congested ISPD'19 testcases that utilize only 5 routing layers. It is noteworthy that different global routers employ various overflow metrics, significantly influencing wirelength and via count. For fair comparison, we adopt the exact overflow metric as presented in CUGR2 [2] when evaluating the results of DGR against those of CUGR2. As illustrated in Table 2, compared with CUGR2, DGR shows a superior routing quality on all testcases : the number of G-cell edges with overflow after global routing is reduced by 23.9%, and the total wirelength and number of vias are also reduced by 0.95% and 1.28% on average.

Moreover, we compare DGR with SPRoute2.0 [8] and Yao [13] on the same ISPD'18 benchmark set as presented in [13]. Both SPRoute2.0 and Yao [13] are leading sequential global routers, showcasing competitive results on the ISPD'18 benchmarks. As shown





the largest case, the GPU used in DGR is NVIDIA A100. ³ The DGR runtime excludes the time required to construct the DAG forest,

a process that can be efficiently accelerated by net-level parallelism. We plan to optimize this aspect when we open source DGR.

in Table 3, The average wirelength is reduced by 2.2% and 4.08% compared with the Yao [13] and SPRoute2.0, respectively. For the vias, even though DGR has more vias than Yao [13] and SPRoute2.0 when the benchmark is small (ispd18_test1 - ispd18_test4), the average number of vias is still reduced by 1.76% and 2.54% since DGR has less via number when the design becomes larger (ispd18_test5 - ispd18_test10).

5.3 Overflow cost function and Scalability Study In global routing, how to model overflow cost is essential for result quality. Here, we represent f in Equation (9) using various functions, namely, ReLU, sigmoid, LeakyReLU, exp, and CELU, respectively. The results are shown in Figure 6. We can see that the selection of f influences the result, especially overflow, significantly, and sigmoid is the best choice, which outperforms CUGR2 (the red X mark) in most cases.

Moreover, we explore the runtime and memory scalability of DGR. As shown in Figure 5a, DGR has slightly more runtime overhead than CUGR2 when the number of nets is less than one million, when the design complexity continues increasing, DGR becomes more efficient than CUGR2. The reason is that DGR can generate better initial routing because of its concurrent global optimization nature, and better initial routing can avoid unnecessary rip-up and reroute. When the design becomes larger, the benefit can mitigate the runtime cost of DGR training. The memory result is given in Figure 5b, which shows that both CPU and GPU memory overhead is almost linear with the number of nets.

6 Conclusion

In this work, we propose a differentiable global router, which enables concurrent optimization over millions of nets, and can be accelerated by deep learning toolkits on GPUs. Experimental results show that our method outperforms the state-of-the-art academic global router on most testcases.

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Table 2: Performance comparison with CUGR2 [2] on the most congested testcases (with 5 routing layers) from ISPD'19 benchmarks, using the same overflow metric as [2].

	В	enchmark	s		# G-cell edges w/ overflow		Total Wirelength		# Vias	
	Cell #	Net #	G-cell Grid	Layer #	CUGR2	DGR	CUGR2	DGR	CUGR2	DGR
ispd18_5m	71954	72394	619 x 613	5	9	7	26748345	26569365	878760	868049
ispd18_8m	192003	179863	905 x 883	5	0	0	62171869	61697029	2182804	2152936
ispd18_10m	290386	182000	606 x 522	5	1	1	74439931	74114344	2311291	2283099
ispd19_7m	359746	358720	1053 x 1011	5	0	0	105264205	104697033	3830903	3802312
ispd19_8m	539611	537577	1202 x 1138	5	14	5	176164609	173050359	6276063	6189202
ispd19_9m	899341	895253	1337 x 1433	5	33	33	262680776	260689064	10438277	10294296
				Ratio	1.2391	1.0000	1.0095	1.0000	1.0128	1.0000

Table 3: Performance comparison with Yao [13] and SPRoute 2.0 [8] on ISPD'18 benchmarks using the exactly same testcases and overflow metric as presented in [13]. The results of Yao [13] and SPRoute 2.0 are from in [13].

D l	# G-cell ed	ges w/ ove	rflow	Tot	al wirelengt	th	# Vias		
Benchmark	SPRoute 2.0	Yao [13]	DGR	SPRoute 2.0	Yao [13]	DGR	SPRoute 2.0	Yao [13]	DGR
ispd18_test1	0	0	0	417181	415116	409081	30460	29677	31683
ispd18_test2	0	0	0	7709980	7699590	7603188	338191	324846	343110
ispd18_test3	0	0	0	8644190	8626810	8531769	336061	326618	347547
ispd18_test4	0	0	0	26246000	26121900	25635347	680322	677125	757225
ispd18_test5	0	0	0	27307600	27183700	26648030	803900	802244	791171
ispd18_test6	0	0	0	35132200	34980000	34249130	1227804	1219063	1182956
ispd18_test7	0	0	0	64964200	64224500	62971368	1979427	1969051	1950290
ispd18_test8	0	0	0	64964200	64224500	63165843	2109296	2082828	1954286
ispd18_test9	0	0	0	53981500	53674000	52504359	1995119	1987919	1937057
ispd18_test10	0	0	0	71709900	67400100	65204874	2182178	2175317	2098285
Ratio	1.0000	1.0000	1.0000	1.0408	1.0220	1.0000	1.0254	1.0176	1.0000



Figure 6: The impact of activation function on the global routing results. Each dot is a single run with different activation functions and different hyper-parametersss. The y-axis (weighted overflow) is calculated as $10 \times n_1 + 1000 \times n_2 + 10000 \times$ peak overflow, where n_1 is the number of nets with overflow after layer assignment, n_2 is the number of G-cell edges with overflow after global routing, peak overflow is the maximum overflow among all G-cell edges.

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